

Bedload transport predictions based on field measurement data by combination of artificial neural network and genetic programming

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ABSTRACT: Bedload transport is an essential component of river dynamics and estimation of its rate is important to many aspects of river management. In this study, measured bedload by Helley- Smith sampler was used to estimate the bedload transport of Kurau River in Malaysia. An artificial neural network, genetic programming and a combination of genetic programming and a neural network were used to estimate the bedload carried in Kurau River, based on bedload transport measurement data and hydraulic variables. A statistical analysis was carried out to validate methods by computing RMSE, MARE and inequality ratio (U). In general, the ability of the artificial neural network combined with genetic programming with R^2 equal to 0.95, RMSE equal to 0.1 as a precipitation predictive tool for predicting the bedload transport rate was observed as being acceptable.

Keywords: Artificial neural network, Bedload transport, Genetic programming, Kurau River

INTRODUCTION

Bedload transport equations are usually developed based on hydraulic principles and attempts are made to relate the level of bedload transport to some correlate of flow, such as water discharge, shear stress or stream power (Martin, 2003). The difficulties associated with bedload field measurement have created a long history of interest in developing equations for the prediction of bedload transport (Gao, 2012; Yadav and Santani, 2008). Due to the relationship between the reliability and representativeness of the data utilized in defining reference values, constants and other relevant coefficients, and the performance of a particular equation, most sediment transport equations do not represent a fundamental or

complete correlation. Therefore it is difficult, if not possible, to recommend a single formula for engineers and geologists to use in the field under all conditions (Camenen and Larson, 2005; Khorram and Ergil, 2010).

River flow condition and river environment have the largest impact on bedload transport rate in different rivers and the computed results from various equations often differ from one another, as well as from the measured data set. Consequently, recently proposed equations need to be adopted for the new condition (Khorram and Ergil, 2010). Nowadays, the new statistical and intelligent methods that have been developed can be used to evaluate or develop the appropriate bedload transport predict equation.

The current study was conducted in six cross-sections of the Kurau River in

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Malaysia, due to the difficulty of sampling and the possibility for wading in the water in these areas. New mathematical modelling methods were used to improve the sensitivity and performance of prediction equations in overcoming the difficulties of developing such equations, and were based on a balance between simplicity and accuracy. Genetic programming (GP) and an artificial neural network (ANN) are powerful tools for pattern recognition and data interpretation.

Multigene GP is in fact a linear combination of nonlinear terms, a characteristic that may precisely identify the pattern of engineering problems (Hinchliffe et al., 1996).

GPTIPS was utilized in this study to perform a multigene GP for the precise estimation of bedload transport. It is a new “genetic programming and symbolic regression” code based on multigene GP for use with MATLAB (Searson, 2009b).

Reported GP applications include sediment transport modelling (Babovic and Abbott, 1997), the effect of flexible vegetation on flow in wetlands (Harris et al., 2003), sedimentary particle settling velocity equations (Babovic and Bojkov, 2001), emulating the rainfall runoff process (Liong et al., 2007; Whigham and Crapper, 2001), an evolutionary computation approach to sediment transport modelling (Kizhisseri et al., 2005), modelling the stage discharge relationship for rivers (Azamathulla et al., 2011) and suspended sediment modelling (Kisi et al., 2012).

Widespread reviews of the ANN application in the area of river engineering show that the model is capable of describing the flow and sediment transport processes in a river system of interconnected channels. In addition, the ANN can be successfully applied for sediment transport when other approaches cannot succeed due to the uncertainty and the stochastic nature of the sediment movement (Chang et al., 2012; Kumar, 2012; Nagy et al., 2002; Singh et al., 2007; Yang et al., 2009).

Among the numerous ANN structures, the multilayer, feed-forward network is the most widely used in the area of sediment transport (Rumelhart et al., 1985). The Levenberg-Marquardt (LM) algorithm, a standard second-order nonlinear least-squares technique based on the backpropagation process, was used in this study to train the ANN models. The performances of the GP and ANN models, as well as a combination of the ANN and GP were evaluated and the best model was selected for estimating the bedload transport of Kurau River.

MATERAIS & METHODS

Site description and data collection

The Kurau River sub-basin (Fig. 1) is between latitude 530 000 (N) and 570 000 (N), longitude 683342 (E) and 723342 (E) in Zone 47 in the UTM coordinate system. The catchment area consists of two main river tributaries, namely Kurau River and Ara River. The mid-valleys of the river are characterized by low to undulating terrain, which gives way to broad and flat floodplains. Ground elevations at the river's headwaters are moderately high at 1200 m and 900 m. The slopes in the upper 6.5 km of the river averages 12.5%, whilst those lower down the valleys are much lower, around the order of 0.25% to 5%.

Data of the six channel criteria were taken along the Kurau River and included a variety sand bed channels. A range of flow discharge measurements covering low and high regimes were carried out using current meter. Measurements taken included flow depth (y_o), velocity (v), river width (B) and water surface slope (S_o) for a detailed analysis of the river.

Bedload and bed material were sampled eight times in each cross-section during the field measurement season. Table 1 shows the range of data measured from the field and the laboratory tests conducted for the fundamental data of the developed models in this study (Table 1).



Fig. 1. Kurau River sub-basin

Table 1. Range of field data

Location	Discharge Q (m^3/s)	V (m/s)	S_o	B m	Y_0 m	A m^2	R (m)	d_{50} (mm)	Bedload Transport T_b (kg/s)
KRU1	3.18-12.79	0.53-0.82	0.0005-0.007	17-19	0.47-1.15	6-15.51	0.412-0.885	0.65-1.044	0.23-2.098
KRU2	1.6-6.1	0.5-0.73	0.0007-0.0185	9-10.3	0.42-1.15	2.87-8.37	0.313-0.76	0.699-1.084	0.168-0.859
KRU3	0.55-1.52	0.31-0.52	0.0006-0.0096	7-9.2	0.28-0.38	1.39-2.89	0.166-0.303	0.99-1.404	0.028-0.265
KRU4	0.56-4.7	0.15-1.22	0.001-0.0062	12-13	0.27-0.52	1.99-6.03	0.161-0.286	1.02-1.83	0.009-0.495
KRU5	2.32-6.6	0.49-1.56	0.0003-0.0051	12-13	0.37-1.03	3.46-9.78	0.224-0.699	0.74-1.51	0.128-1.515
Ara1	0.77-5.25	0.4-0.69	0.0003-0.0312	11.3-13	0.27-0.86	1.94-7.57	0.167-0.567	1.29-1.84	0.116-1.04

Artificial neural networks (ANN)

A neural network toolbox contained within the MATLAB package was used in this study. Bedload transport equations were integrated into a multilayer feed-forward network with an error backpropagation algorithm. Field data were provided and an appropriate neural network structure was selected for training purposes. Training was performed using Levenberg-Marquardt backpropagation, where input and output were presented to the neural network as a series of learning. The network was set up with four parameters: the input pattern of discharge (Q), water surface slope (S), mean grain size (d_{50}) and Shields parameter for the initiation of motion (θ), as these are the most influential parameters widely used in bedload transport equations; bedload transport rate T_b was applied as the output pattern. In other words, the input

layer contained four neurons while the output layer contained one. Between the two layers, there was another hidden layer that contained a suitable number of neurons under investigation.

Genetic programming method (GP)

A GPTIPS run was performed with the following settings: population size = 500; number of generations= 25; tournament size= 7 (with lexicographic selection pressure); $D_{max}= 3$; $G_{max}= 4$; elitism 0.0% of the population; function node set = (plus, minus, times, protected). The default GPTIPS multigene symbolic regression function was used in order to minimize the root mean squared prediction error for the training data (Searson, 2009a). These settings are not considered ‘optimal’ in any sense, but were based on experience with modelling different data sets of similar size.

The selection of appropriate model input variables in GP, as with any data-driven prediction model, is extremely important. The choice of input variables is generally based on previous knowledge concerning the most influential variables, as well as insight into the problem (Khorram and Ergil, 2010). Four input parameters, including discharge(Q), water surface slope (S), mean grain size (d_{50}) and Shields parameter for the initiation of motion (θ) as the most influential parameters have been widely used in bedload transport equations as variable data, with T_b (bedload transport rate) as invariable data being used in the current study, where :

$$T_b = f(Q, S, d_{50}, \theta) \quad (1)$$

RESULTS & DISCUSSION

Prediction of bedload transport in Kurau River by genetic programming

Multiple sets of training, testing and validation data were randomly selected and numerous runs were performed with various model settings, such as the number of generation and genes, and the depth of trees by the trial and error. From 69 available data, 50% were used for training (present study), 25% were used for testing and 25% (DID, 2009) for validation. Consequently, the models were selected according to statistical criteria such as R^2 and RMSE.

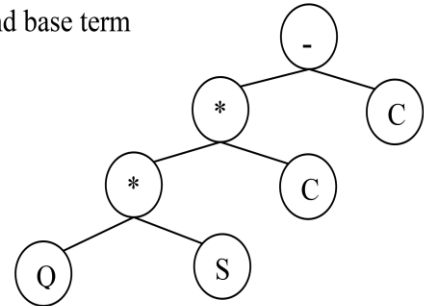
The best relationship for each training purpose, test and validation was selected from the optimum R^2 and RMSE so as to prevent from over-fitting the model by selecting a high R^2 for training. The following relationship was selected to model the bedload transport:

$$T_b = 0.09427 Q + 35.81 S + 0.06682 Q (d_{50} + \theta) - 38.02 Q S - 0.06172 \quad (2)$$

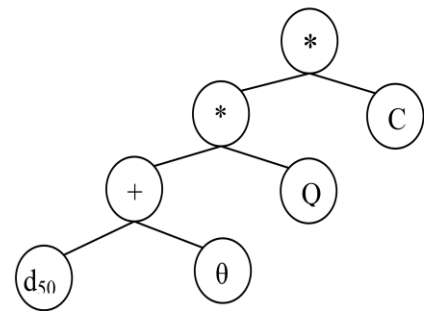
where T_b is bedload transport rate (kg/s), d_{50} is median grain size (mm), S water surface slope (m/m) and θ is Shield's parameter. Figure 2 shows the expression of genes for GP formulation.

The accuracy of the developed equation was examined by plotting the measured versus predicted values of bedload rate for training, testing and all other data. The values of R^2 and RMSE were equal to 0.96 and 0.083, respectively, for training sets, and 0.78 and 0.159, respectively, for testing sets.

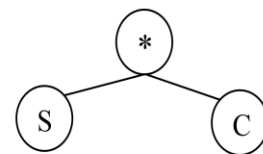
Gene 1 and base term



Gene 2



Gene 3



Gene 4

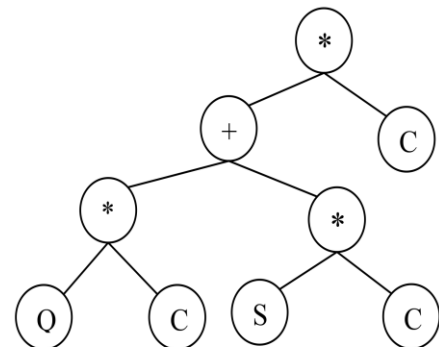


Fig. 2. Expression genes for GP formulation

The predictive abilities of the GP (Eq. 2) were assessed through the validation of the model by the set of data gathered about the Kurau River of the present study, as well as data from a previous study (DID, 2009). The values of R^2 and RMSE for this data set were obtained as being equal to 0.89, 0.110, respectively. In fact, the evolved model achieved good accuracy for both testing and validation sets, thereby confirming that enough generalization had been obtained.

Combination of ANN and GP

The combination of GP and ANN was suggested for achieving the best result for predicting sediment transport (Singh et al., 2007). The combination of GP and ANN was performed for the modelling of bedload transport rate in Kurau River.

First, the bedload transport rate was calculated using the GP Equation (2) and then the outcome was given as an input to the ANN, which consisted of one input node, one output node and 10 hidden layers. Figure 3 shows the test result in the

form of a scatter plot of predicted against measured bedload transport. The underlying error measures were $R^2= 0.92$ and $RMSE= 0.11$ kg/s. The results showed that the combination of GP-ANN can be applied to provide predictions of bedload transport rate and, not surprisingly, performed better than GP application. Alternatively, a neural network consisting of the input of four variables (Q, S, d_{50}, θ) and one output T_b was trained and validated. For this purpose, the data were shuffled and divided into two parts; one part was randomly applied in the learning process, while the other part was used for verification. This can often be done in more than one way by changing the percentage of data for the training process and verification. Finally, from 69 available data aspects, 50% were used for training and 25 % were used for testing and validation. The number of neurons in the hidden layer was determined by calibration using several computer-applied tests on random data sets.

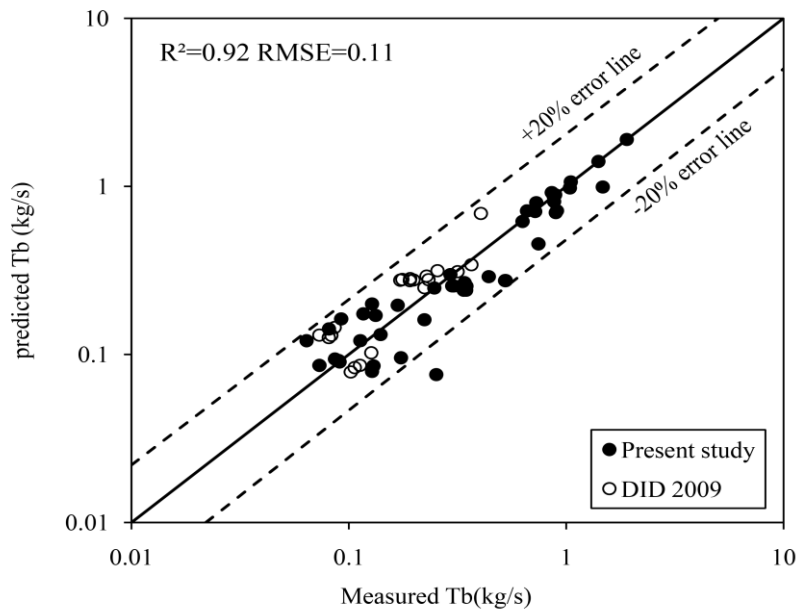


Fig. 3. Measured versus predicted values of T_b by GP-ANN

The correlation of determination, root mean square error and mean absolute error of training, testing and the validation of

modelling are shown in Table 2. The results indicate that an acceptable network was obtained, but not an acceptable GP.

Table 2. Summary of ANN results

Data	Percentage of total data	R ²	RMSE	MAE
Training	50%	0.9	0.16	0.088
Testing	25%	0.81	0.16	0.013
Validation	25%	0.9	0.10	0.085
Total	100%	0.86	0.15	0.1

The outcome of the ANN was calibrated with GP and the result showed an expected success and an improved R², as well as the indicating errors (R²= 0.94, RMSE= 0.1

and MARE= 0.32). The plot scatter of the measured against predicted bedload transport rate is shown in Figure 4.

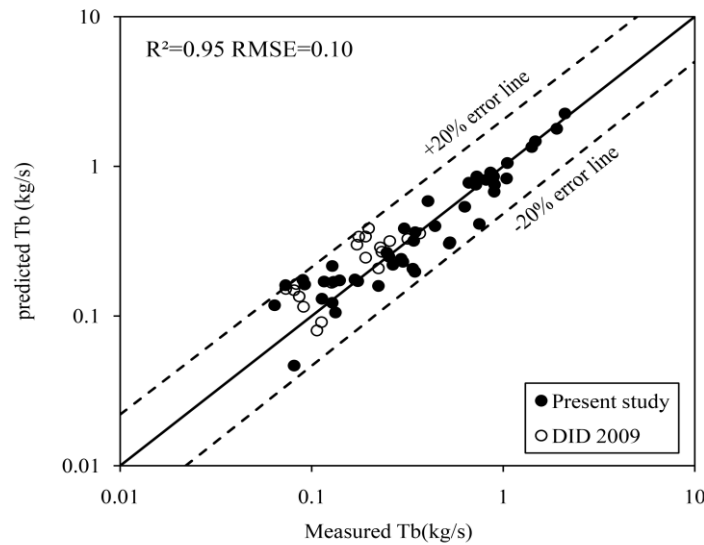


Fig. 4. Measured versus predicted values of T_b by ANN-GP

The combined ANN-GP model results therefore appear to be more acceptable than those of the single ANN and GP models. The combination showed that, firstly, the ANN carried out a good function approximation; thereby, GP made the search for an optimum solution easier and improved the accuracy of the single

ANN and GP results. This method was validated by some river data from a previous study in Malaysia (Table 3). Figure 5 shows the high accuracy of the ANN-GP method, with R²= 0.80 and RMSE= 0.14 for estimation of bedload transport rate in some rivers in Malaysia.

Table 3. Range of field data for validating the GP equation (Yahaya, 1999; Ab. Ghani et al., 2003; Chang et al., 2008)

River	No of data	Discharge	Slope	Width	Water Depth	Hydraulic radius	Median size	Bedload transport
		Q (m ³ /s)	S ₀ (m/m)	B (m)	Y ₀ (m)	R _h (m)	d ₅₀ (mm)	T _b (kg/s)
Kampar River	20	7.98-17.94	0.001	20.2-21.21	0.55-1.28	0.52-1.14	0.85-1.10	0.40-1.25
Raia River	40	3.6-17.44	0.0017-0.0036	17.3-25.6	0.24-1.76	0.23-1.51	0.50-1.60	0.20-1.82
Kinta River	20	3.79-9.65	0.0011	24.6-28.0	0.32-0.57	0.35-0.57	0.40-1.00	0.02-1.21
Pari River	40	9.65-17.4	0.0012-0.0013	19.3-19.5	0.68-0.89	0.54-1.30	0.85-3.10	0.35-0.79
Kulim River	20	0.73-14.15	0.001	9-19	0.20-0.91	0.20-0.58	1.00-2.40	0.06-0.36

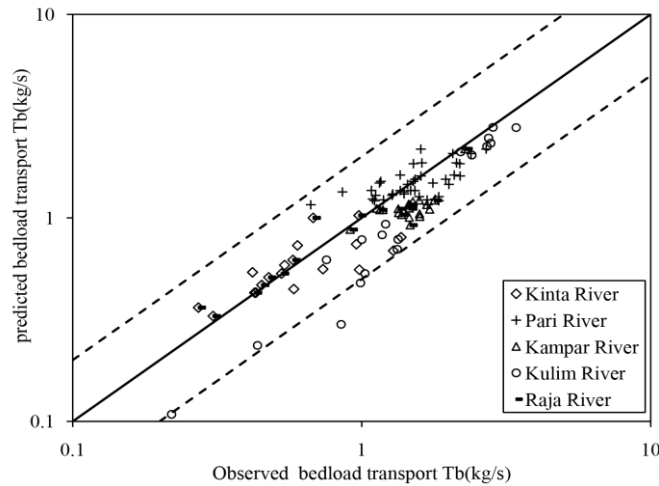


Fig. 5. Validation of ANN-GP method by river data sets in Malaysia

Comparison of bedload transport estimation for Kurau River

Three conventional evaluation criteria, RMSE (root mean square error), mean absolute relative error (MARE) and U (inequality coefficient) were used in the present study to measure the performances of models based on training data and testing data.

RMSE provides a quantitative indication of the model absolute error in terms of the units of the variable, with the characteristic that larger errors receive greater attention than smaller ones. This characteristic can help eliminate approaches with significant errors (Wu et al., 2008). For MARE, answers were provided as the percentage error in predictions. The inequality coefficient (*U*) was used to determine how accurate a bedload equation predicted the actual value of bedload discharge in the Kurau River in similar bedload-transport conditions. The inequality coefficient (*U*) is defined as:

$$U = \frac{rmse}{\left[\frac{1}{n} \sum_{i=1}^n (T_{bo})_i^2 \right]^{1/2} + \left[\frac{1}{n} \sum_{i=1}^n (T_{bp})_i^2 \right]^{1/2}} \quad (3)$$

where RMSE is the root-mean-square error, defined as

$$RSME = \left[\sum_{i=1}^n \frac{(T_{bo} - T_{bp})_i^2}{n} \right]^{1/2} \quad (4)$$

$$MARE = \frac{1}{n} \sum_{i=1}^n \left| \frac{T_{boi} - T_{bpi}}{T_{boi}} \right| \quad (5)$$

where T_{bi} is the measured bedload rate, T_{bo} is the predicted bedload rate, i denotes a given flow and n is the number of flows. The scaling of the denominator is such that U always fall between 0 and 1. If $U = 0$, then $T_{bi} = T_{bo}$ and there is a perfect fit. If $U = 1$, then $T_{bo} \neq T_{bp}$ and the equation lacks a predictive value. For the purpose of this study, the GP and NLR methods represented the measured data when U was very small and close to 0 (Table 4).

Table 4. Bedload estimations assessment

Models	Coefficient of determination (R^2)	Root mean square error (RMSE)	Mean absolute error (MAE)	Inequality coefficient (U)
GP	0.90	0.0829	0.0807	0.068
ANN	0.86	0.15	0.100	0.083
ANN-GP	0.95	0.10	0.075	0.09
GP_ANN	0.92	0.11	0.073	0.082

The results were also tested against the unreliability of the methods applied. Cronbach's alpha (Cronbach, 1951) is a coefficient of internal consistency that is used as an estimate of the reliability of the results of applied methods. The observed transport data were a best fit with a combination of ANN- and GP-based results with reliability of 0.98 of Cronbach's α .

Figure 6 demonstrates the observed versus predicted transport rates of the Kurau River study sites and indicates that predicted values by GP, GP-ANN, ANN and ANN-GP methods were typically within an order of magnitude for the observed values. However, the ANN-GP model showed better performance with 0.95 as the correlation coefficient.

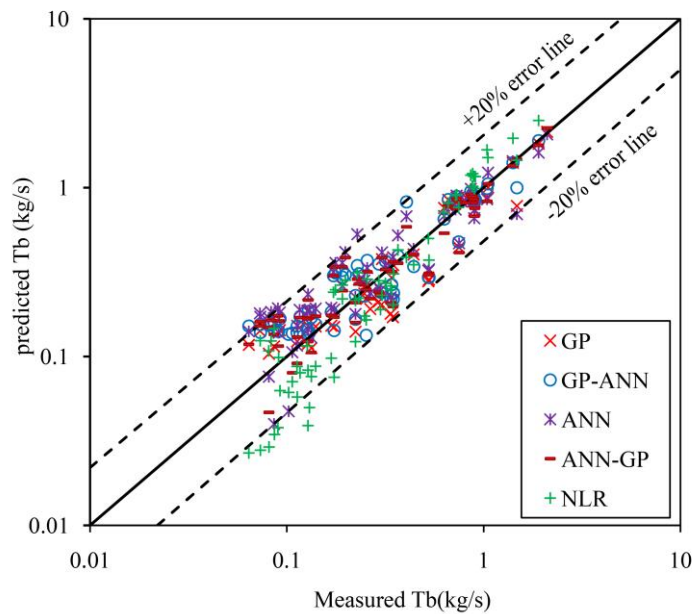


Fig. 6. Comparisons of predicted and measured bedload rates for Kurau River

CONCLUSION

Hydraulic variables and sediment data from Kurau River in Malaysia were used to predict bedload transport. The artificial neural network and genetic programming methods were used and the RSME and inequality ratio ($U < 0.1$) suggested good agreement between the computed and predicted bedload transport rate for Kurau River. The developed model by combination of ANN-GP, compared to GP and ANN, showed reasonable performance under field conditions according to the verifications demonstrated in Figure 6. From the results of bedload prediction with $R^2 = 0.95$, root mean square error (RMSE = 0.1) and mean absolute error (MARE = 0.32), respectively, it can be concluded that the combination ANN-GP

model provides a good fit for the measured data. The combined ANN-GP model results therefore appear to be more acceptable than the results of a single ANN or GP model in the context of this study and in comparison with other methods such as adaptive neuro-fuzzy inference system (ANFIS) ($R^2 = 0.648$, RMSE = 6.654) for the prediction of total bed material load for three Malaysian rivers (Chang et al., 2012). The combination model showed that the ANN first carries out a good function approximation, thereby enabling GP to make the search for an optimum solution easier and improving the accuracy of single ANN and GP results.

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